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PROPAGATION EFFECTS IN DISTURBED ENVIRONMENTS



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	Radio beacon diagnostics are still the least expensive means of obtaining data on naturally occurring and artificially induced striations. To exploit this capability fully, we develop the theory for interpreting rocket-beacon data when the velocity component along the line of sight to the receiver is much larger than the transverse component. A simple and direct				
	relationship is shown to exist between the beacon-phase spectrum and the one-dimensional in-situ spectrum that does not involve any unknown parameters, such as the path length within the disturbance.				

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TABLE OF CONTENTS

Section		Page
	LIST OF ILLUSTRATIONS	2
I	INTRODUCTION	3
II	RADIO-BEACON MEASUREMENTS OF LOCAL	,
	IRREGULARITY STRUCTURES	6
	A. Background	6
	B. Spectral Relations for Rocket-Beacon Phase Measurements	8
III	DOPPLER SPECTRUM	20
	A. Background	20
	B. Special Cases and Numerical Computations	24
IV	CONCLUSIONS	28
	REFERENCES	29

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NTIS	GRA&I				
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Justification					
Ву					
Distribution/					
Availability 68das					
L	Avail an	4/8 F			
Bist	Special	£			
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LIST OF ILLUSTRATIONS

Figure		Page	
1	Region of $\kappa_{v}^{\prime} - \kappa_{z}^{\prime}$ Plane Where $1/L D_{L} $ Can be		
	Approximated by sinc ²	15	
2	Perspective Plot Showing $1/L\left D_L^{}\right ^2$ as a Function		
	of κ' and κ' for small β and large κ	16	
3	Perspective Plot Showing the Effect of Decreasing ${\bf k}_{\bf z}$	17	
4	Perspective Plot Showing the Effect of Increasing β	19	
5	Variation of Structure Function Expansion Coefficient		
	with Changing Spectral Index	23	
6	Doppler Spectrum for Shallowly Sloped Phase Spectra	26	
7	Doppler Spectrum for		
	More Steeply Sloped Phase Spectra	27	

I INTRODUCTION

Theoretical work in wave propagation in randomly irregular media has progressed considerably over the last several years [Flatté et al., 1980; Rino et al., 1980b; Rino, 1980]. A collection of comparatively simple formulas has emerged that characterize the most important channel effects—temporal coherence loss, frequency coherence loss, and angle scattering,—under conditions of strong scattering, such as would occur in the ionosphere following a high-altitude nuclear detonation. To the extent that these results have been tested, they have proven accurate.

Insofar as basic, theoretical work on propagation is concerned little more is required for predicting system performance in highly disturbed, but known propagation environments. The basic problem of accurately characterizing such propagation environments remains, however, and new issues continue to emerge. For example, in the power-law environments that seem characteristic of all turbulent channels, the severity of the propagation effects are sensitive to changes in the spectral index. To study such subtle effects, a refined propagation theory is important because "channel sounding" remains the most economical means of obtaining data on irregularity structures. Under this contract, we have investigated a new technique for beacon diagnostics.

For some time there has been concern about the accuracy with which the scintillation structure "mirrors" the underlying irregularity structure that causes the scintillation. This concern was intensified when the Wideband satellite data showed a spectral index that was not only shallower than was expected, but also variable. This dilemma has only recently been resolved by carefully analyzing data from the Atmospheric Explorer Satellite E (AE-E)[Livingston et al., 1980]. These data showed that the in-situ spectral index is indeed more

shallowly sloped than expected and that it varies systematically, as the Wideband satellite data implied.

In addition to the shape of the spectral density function (SDF), we would like to measure the absolute electron-density fluctuation level or turbulent strength (as distinct from IN/N) for each spectral component. To do so from conventional phase-scintillation data involves a two-fold complication:

- (1) The level of phase-scintillation depends on the propagation geometry relative to the principal irregularity axis of elongation and the corresponding "stretch" factors or axial ration.
- (2) The level of phase-scintillation depends on the integral along the propagation path.

Because the irregularity anisotrophy, the path length of, and, in particular, the structure variation along the propagation path are a priori unknown, a completely unambiguous determination of turbulent strength from such scintillation data is not feasible.

In the DNA PLUMEX experiment conducted at Kwajalein during July-August 1979, however, a downward-looking radio beacon was flown together with a sophisticated complement of in-situ probes. Unlike the satellite-beacon measurements, in the rocket configuration the velocity component along the line of sight is much larger than the transverse component. A comparative analysis of the in-situ probe and beacon data from PLUMEX has shown that there is a simple derivative relationship between the beacon phase and the in-situ density that does not involve any unknown parameters [Rino et al., 1980; Petriceks, 1980]. Thus, the beacon data can be used to determine the turbulent strength.

Because of the comparative simplicity of such rocket-beacon measurements, we have developed a theory (Section II of this report)

for interpreting rocket beacon-phase spectra where $v_{\parallel} >> v_{\perp}$. The results show that as long as β = $v_{\parallel}/v_{\parallel}$ is less than \sim 40 percent,

$$\Phi_{\mathbf{z}}(\kappa) = \mathbf{r}_{\mathbf{e}}^{2} \lambda^{2} \Phi_{\mathbf{1}}(\kappa) / \kappa^{2}$$

where $\Phi_{\mathbf{Z}}(\kappa)$ is the beacon-phase SDF and $\Phi_{\mathbf{1}}(\kappa)$ is the one-dimensional SDF as measured by the in-situ probe. The relationship obviously breaks down at small wave numbers, but the analysis shows that, depending on β , the relationship holds to within a few spectral resolution cells of the smallest resolvable Fourier component. Because the classical electron radius, $\mathbf{r}_{\mathbf{e}}$, and the wavelength, λ , are known, the beacon-phase SDF can be simply and unambiguously related to the in-situ SDF. The technique is, therefore, potentially useful for future diagnostic rocket probes.

In Section III of this report, we have investigated the simplest form of the mutual coherence function, which is useful for modeling the Doppler spectrum of a scintillating signal. An approximate formula is developed that relates the perturbation strength to the spectral width without having to evaluate gamma functions. Two limiting analytic forms for the Doppler spectrum are derived: one characterizes shallowly-sloped phase spectra and has a power-law form; the second has a Gaussian form and is appropriate for more steeply-sloped spectral-density functions. Numerical computations are presented that show the variation of the spectral shape with changing the spectral index between the two extremes where analytic results can be obtained.

These results are useful for both predictive modeling and data analysis. The Doppler spectral model is being verified concurrently using Wideband satellite data.

II RADIO-BEACON MEASUREMENTS OF LOCAL IRREGULARITY STRUCTURES

A. Background

Over the last decade, extensive phase scintillation data have been obtained from low orbiting and geosynchronous satellites [Crane, 1977; Davis et al., 1975; Rino et al., 1980b]. In such measurements both the signal source and receiver are generally well removed from the disturbed medium. Ignoring diffraction effects and temporal changes in the medium, the instantaneous phase perturbation is given by the formula

$$\phi(t) = kR(t) - r_e^{\lambda} \int_0^{\ell} N_e(\dot{v}_1^t, \eta) d\eta \qquad , \qquad (1)$$

where k = $2\pi/\lambda$, R(t) is the range to the satellite, ℓ_p is the length of the propagation path within the disturbed medium, and $N_e(\vec{\rho}, z)$ is the local electron density.

The path length changes with time, but ℓ_p is assumed nearly constant over periods long compared to the time scale for phase changes of interest. If $v_p = v_p \hat{a}_p$, the phase SDF takes the form

$$\Phi(\mathbf{f}) = \mathbf{r}_{e}^{2} \lambda^{2} \ell_{p} \int_{-\infty}^{\infty} \Phi\left(\kappa_{x}, \frac{2\pi \mathbf{f}}{v_{y}}, 0\right) \frac{d\kappa_{x}}{2\pi} , \qquad (2)$$

where $\phi(\kappa, \kappa_z)$ is the three-dimensional SDF of $N_e(\rho, z)$. The corresponding one-dimensional SDF measured by an in-situ probe is

$$\phi_{1}(f) = \int \int_{-\infty}^{\infty} \phi\left(\kappa_{x}, \frac{2\pi f}{v_{y}}, \kappa_{z}\right) \frac{d\kappa_{x}}{2\pi} \frac{d\kappa_{y}}{2\pi} . \tag{3}$$

It is readily shown [Rino, 1979] that if $\phi(\kappa, \kappa_Z) \propto q^{-(2\nu+1)}$, then $\phi(f) \propto f^{-2\nu}$ and $\phi_1(f) \propto f^{-(2\nu-1)}$. Thus, if $\nu = 1.5$, then the phase SDF has the power-law form f^{-3} , whereas the one-dimensional in-situ has the power-law form f^{-2} . The difference of unity between the in-situ and phase spectral indices has been verified by comparing spectral measurements derived from Wideband satellite phase data and AE-E in-situ data [Livingston et al., 1980].

For a downward-looking, rocket-borne radio beacon, the signal phase takes the form

$$\phi(t) = k(z_0 + v_z t) - r_e \lambda \int_{0}^{z_0 + v_z t} N_e(\vec{v}_1 t, \eta) d\eta \qquad , \tag{4}$$

where $\mathbf{v}_{\mathbf{z}}$ and $\overset{\rightarrow}{\mathbf{v}_{1}}$ are the relative velocity components along and transverse to the line of sight to the receiver. The fixed path length \mathbf{z}_{0} effectively establishes the initial condition for the indefinite integral that $\mathbf{v}_{\mathbf{z}}$ t maps out.

In the early development of guided missiles, radio-beacon measurements were used for trajectory evaluation. As with satellite radio navigation, the ionospheric contribution was a source of error. As the techniques were refined, however, the radio-beacon data came to be used to determine ionospheric density profiles [Berning, 1951]. If \mathbf{v}_1 is small, we have only to remove the geometric Doppler term $\mathbf{k}\mathbf{v}_2$ t in Eq. (4) and differentiate the residual to obtain $\mathbf{N}_{\mathbf{e}}(\mathbf{z})$. Note that the measurement gives absolute electron density because only phase changes are involved.

More recently, the technique has been exploited to measure small-scale irregularity structure. In July 1979, a rocket-borne radio beacon was launched from Roi Namur Island in the Kwajalein Atoll into a highly disturbed equatorial ionosphere. The results

of the beacon and probe structure comparisons are described in Rino et al. [1980c]. The data interpretation was based on the assumption that \mathbf{v}_1 in Eq. (4) could be disregarded. This assumption was justified ex post facto by the agreement between the in-situ and beacon data.

In this section we develop the theory, in detail, to assess the general applicability of the radio-beacon measurement technique for determining local in-situ irregularity structures. We begin by computing the general relation between the beacon-phase SDF and $\mathbb{P}(\hat{r}, |r_2)$.

B. Spectral Relations for Rocket-Beacon Phase Measurements

To simplify notation, we let $\mathbf{z} = \mathbf{v}_{\mathbf{z}} \mathbf{t}$ and consider the indefinite integral

$$N_{T}(z) = \int_{0}^{z_0+z} N_{e}(\hat{\beta}z, \eta) d\eta \qquad , \qquad (5)$$

where

$$\dot{v} = \dot{v}_1 / v_z \qquad . \tag{6}$$

If we assume that $N_e(\cdot, z)$ can be modeled by a statistically homogeneous random process throughout the measurement region, we can write

$$N_{e}(\vec{x}, z) = \iiint \exp \left\{-i\left(\vec{x} + z\right)\right\} d\xi_{N}(\vec{x}, +z) , \qquad (7)$$

where

$$\langle d\xi_{N}(\vec{k}, k_{z})d\xi_{N}*(\vec{k}, k_{z})\rangle = \frac{1}{(2\pi)^{3}} + (\vec{k}, k_{z})\delta(\vec{k} - \vec{k})\delta(k_{z} - k_{z})$$
(8)

is a purely formal definition of the orthogonal increments property of the Fourier spectrum $d\xi_N(\dot{\kappa},+\frac{1}{2})$.

By substituting Eq. (7) into Eq. (5) and changing the order of integration, we can eliminate the indefinite integral in Eq. (5). The result is

$$N_{T}(z) = \iiint \exp\left\{-i \cdot \hat{\beta}_{z}\right\} \left[\frac{\exp\left\{-i \cdot \hat{\beta}_{z}(z+z_{0})\right\} - 1}{-i \cdot z}\right] d\xi_{N}(\hat{\beta}_{z}, +z_{0}) \qquad (9)$$

Because we can only compute the finite Fourier transform, we shall only consider the integral

$$\hat{N}_{T}(\cdot_{z}) = \int_{0}^{L} N_{T}(z) \exp\left\{i\cdot_{z}z\right\} dz \qquad (10)$$

In fact, $N_T(z)$ must be modified to avoid contamination of the spectral estimate because of "end point mismatch." Such subtleties need not be formally carried through the analysis, however.

If Eq. (9) is now substituted into Eq. (10) and the integration over z performed, the result is

$$\hat{N}_{T}(\kappa_{z}) = \iiint \exp\{-i\kappa_{z}'z_{0}\} (\kappa_{z}', \kappa_{z}', \kappa_{z}; z_{0}) \frac{d\ell_{N}(\kappa_{z}', \kappa_{z}')}{+z} .$$
 (11)

where

$$D_{L}(q_{1}, q_{2}, q_{3}; z_{0}) \stackrel{\triangle}{=} \left[\frac{\exp\left\{-i\left(q_{1} + q_{2} - q_{3}\right)L\right\} - 1}{\left(q_{1} + q_{2} - q_{3}\right)} - \exp\left\{iq_{2}z_{0}\right\} \right]$$

$$\times \frac{\exp\left\{-i(q_{1}-q_{3})L\right\}-1}{(q_{1}-q_{3})} \qquad (12)$$

An estimate of the SDF of N $_{T}(z)$ is obtained by computing $|\hat{N}_{T}(\kappa_{z})|^{2}/L$ and averaging to smooth the statistical fluctuations. The result is close to the expectation value,

$$\hat{\Phi}_{z}(\kappa_{z}) = \langle |\hat{N}_{T}(\kappa_{z})|^{2} \rangle / L \qquad (13)$$

To evaluate Eq. (13), we substitute $\hat{N}_T(\kappa_z)$ from Eq. (11) and use the orthogonal increments property Eq. (8) to obtain

$$\Phi_{\mathbf{z}}(\kappa_{\mathbf{z}}) = \iiint \frac{1}{L} \left| D_{\mathbf{L}}(\kappa', \kappa_{\mathbf{z}}, \kappa_{\mathbf{z}}, \kappa_{\mathbf{z}}; z_{0}) \right|^{2} \frac{\Phi(\kappa', \kappa_{\mathbf{z}}')}{\kappa_{\mathbf{z}}^{2}} \frac{d\kappa'}{(2\pi)^{2}} \frac{d\kappa'}{2\pi} . \tag{14}$$

We note that there is no singularity at κ_z' = 0 because

$$\lim_{\kappa_{z}^{\prime} \to 0} D_{L}(\vec{\kappa}^{\prime} \cdot \vec{\beta}, \kappa_{z}^{\prime}, \kappa_{z}^{\prime}; z_{0}) \kappa_{z}^{\prime - 2} = \frac{\sin^{2}[(\vec{\kappa}^{\prime} \cdot \vec{\beta} - \kappa_{z}^{\prime})L/2]}{(\vec{\kappa}^{\prime} \cdot \vec{\beta} - \kappa_{z}^{\prime})^{2}} . \quad (15)$$

Let us first consider the special case for which β = 0. Then,

$$\hat{\Phi}_{z}(\kappa_{z}) = \int_{-\infty}^{\infty} \frac{1}{L} \left| D_{L}(0, \kappa_{z}, \kappa_{z}; z_{0}) \right|^{2} \frac{\Phi_{1}(\kappa_{z})}{\kappa_{z}^{2}} \frac{d\kappa_{z}}{2\pi} , \qquad (16)$$

where

$$\Phi_{1}(\kappa_{z}) = \int_{-\infty}^{\infty} \int \Phi(\vec{\kappa}, \kappa_{z}) \frac{d\vec{\kappa}}{(2\pi)^{2}}$$
 (17)

is the one-dimensional spatial SDF derived from a probe scanning along the z axis which should not be confused with the temporal SDF defined by Eq. (3).

The general behavior of Eq. (16) is readily established. We first isolate the κ_Z^\prime regime where Eq. (15) applies. It is sufficient to take κ_Z^\prime < $2\pi/L$, whereby

$$\int_{\overline{L}}^{1} \left| D_{L}(0, \kappa_{z}, \kappa_{z}; z_{0}) \right|^{2} \frac{\Phi_{1}(\kappa_{z})}{\kappa_{z}^{2}} \frac{d\kappa_{z}}{2\pi}$$

$$|\kappa_{z}| < 2\pi/L$$

$$< \frac{\sin^{2} \left[\kappa_{z} L/2\right]}{\kappa_{z}^{2} L} \int_{1}^{\Phi_{1} \left(\kappa_{z}^{2}\right)} \frac{d\kappa_{z}^{2}}{2\pi} . \tag{18}$$

This contribution to Eq. (16) becomes vanishingly small as $\kappa_{_{\rm Z}}$ increases; however, for large $\kappa_{_{\rm Z}}$

$$\frac{1}{L} \left| D_{L}(0, \kappa_{z}^{2}, \kappa_{z}; z_{0}) \right|^{2} \approx \frac{\sin^{2} \left[(\kappa_{z} - \kappa_{z}^{2}) \frac{L}{2} \right]}{(\kappa_{z} - \kappa_{z}^{2})^{2} L} . \tag{19}$$

Now, as long as the variation of $\Phi_1(\kappa_z)$ is small over κ_z intervals, comparable to $2\pi/L$, we can show that

$$\int \frac{\sin^2\left[\left(\kappa_z - \kappa_z^{\prime}\right) \frac{L}{2}\right]}{\left(\kappa_z - \kappa_z^{\prime}\right)^2 L} \frac{\phi_1(\kappa_z^{\prime})}{\kappa_z^{\prime 2}} \frac{d\kappa_z^{\prime}}{2\pi} \cong \frac{\phi_1(\kappa_z)}{\kappa_z^{\prime 2}}$$

$$\left|\kappa_z^{\prime}\right| \ge 2\pi/L \tag{20}$$

[Rosenblatt, pp. 169-180, 1962], which is sometimes referred to as the "sifting property" of $sinc^2$.

As long as $\kappa_{_{\mbox{\scriptsize Z}}} \geq 2\pi/L$, the β = 0 behavior of Eq. (14) is summarized by

$$\hat{\Phi}_{\mathbf{z}}(\kappa_{\mathbf{z}}) \cong \Phi_{\mathbf{1}}(\kappa_{\mathbf{z}})/\kappa_{\mathbf{z}}^{2} \qquad . \tag{21}$$

The relationship Eq. (21) is useful because it involves no unknown paramters, e.g., the length of the propagation path or the axial ratios, which characterize the anisotropy of the medium.

At the opposite extreme where β is very large, we can disregard q_2 in Eq. (12) where is appears next to q_1 . The result is

$$\hat{\Phi}_{z}(\kappa_{z}) \cong \iint \frac{\sin^{2}\left[\left(\kappa^{2}, \frac{1}{\beta} - \kappa_{z}\right)L/2\right]}{\left(\kappa^{2}, \frac{1}{\beta} - \kappa_{z}\right)2L}$$

$$\times \int_{-\kappa_{z}^{2}}^{\infty} \frac{\sin^{2}\left[\kappa_{z}^{2} z_{0}/2\right]}{\kappa_{z}^{2}} \Phi\left(\vec{\kappa}; \kappa_{z}^{2}\right) \frac{d\kappa_{z}^{2}}{2\pi} \frac{d\vec{\kappa}}{(2\pi)^{2}} . \tag{22}$$

In the usual approximation the integral over κ_z is replaced by $z_0^{\frac{1}{4}(\kappa_z^2;0)}$. Finally, by letting $\hat{\beta} = \beta \hat{a}_y$ and applying the sifting property of sinc $\frac{1}{2}$ to the κ_y integration, we have

$$\Phi_{\mathbf{z}}(\kappa_{\mathbf{z}}) \cong \mathbf{z}_{0} \int_{0}^{\infty} \Phi(\kappa_{\mathbf{x}}, \, \beta \kappa_{\mathbf{z}}, \, 0) \, \frac{d\kappa_{\mathbf{x}}}{2\pi} \qquad , \tag{23}$$

which is essentially equivalent to Eq. (2). Note that z_0 in Eq. (23) is the distance from the point where the disturbance starts and is, therefore, unknown.

For $0 < \beta < 1$, which is the case of primary interest, we first isolate the region near $\frac{1}{z} = 0$ and use Eq. (15). In place of Eq. (18) we now have

$$\iiint_{-\infty}^{\infty} \left[\int_{|\vec{\kappa} \cdot \vec{\beta}| < 2\pi/L} \frac{d\vec{\kappa}_{z}}{(2\pi)^{2}} \frac{d\vec{\kappa}_{z}}{2\pi} \approx \int_{-\infty}^{\infty} \frac{\sin^{2} \left[(\vec{\kappa} \cdot \vec{\beta} - \kappa_{z}) L/2 \right]}{(\vec{\kappa} \cdot \vec{\beta} - \kappa_{z}) 2L} \right]$$

$$\int \phi(\vec{\kappa}; \kappa_{z}) \frac{d\vec{\kappa}}{(2\pi)^{2}} \frac{d\kappa_{z}}{2\pi} .$$

$$|\kappa_{z}'| < 2\pi/L$$
(24)

If we let $\vec{\beta} = \hat{\beta a}_y$ and using the sifting property of sinc², the right-hand side of Eq. (24) can be replaced by

$$\int\int_{-\infty}^{\infty} \frac{1}{\beta} \, \Phi(\kappa_{\mathbf{x}}', \kappa_{\mathbf{z}}') \, \frac{d\kappa_{\mathbf{x}}'}{2\pi} \, \frac{d\kappa_{\mathbf{z}}'}{2\pi} \, . \tag{25}$$

For a power-law SDF this contribution again decreases rapidly with increasing $\kappa_{_{\mbox{\scriptsize 2}}}.$

The behavior of Eq. (14) for the region outside $|\kappa_z'| < 2\pi/L$ can be determined with the aid of Figure 1 where the $\kappa_y' - \kappa_z'$ plane has been partitioned into two regions separated by the line $\kappa_y' = \kappa_z'/\beta$. To the right of this line,

$$\frac{1}{L} \left| D_{L}(\vec{\kappa}' \cdot \vec{\beta}, \kappa_{z}', \kappa_{z}; 0) \right|^{2} \cong \frac{\sin^{2} \left[(\vec{\kappa}' \cdot \vec{\beta} + \kappa_{z}' - \kappa_{z}) L/2 \right]}{(\vec{\kappa}' \cdot \vec{\beta} + \kappa_{z}' - \kappa_{z}) 2L} \qquad (26)$$

The lines where Eq. (26) achieves its maximum value are also shown in Figure 1. This behavior is illustrated in the perspective plots of $\frac{1}{L} \left| \mathbf{D}_L(\kappa_y^*\beta, \kappa_z^*, \kappa_z^*; 0) \right|^2$ shown in Figures 2 and 3. For convenience, L was set equal to 2. Figure 2 corresponds to a large κ_z value so that the shaded region $\kappa_y^* < \kappa_z^*/\beta$ is not entered over the κ_y^* range plotted.

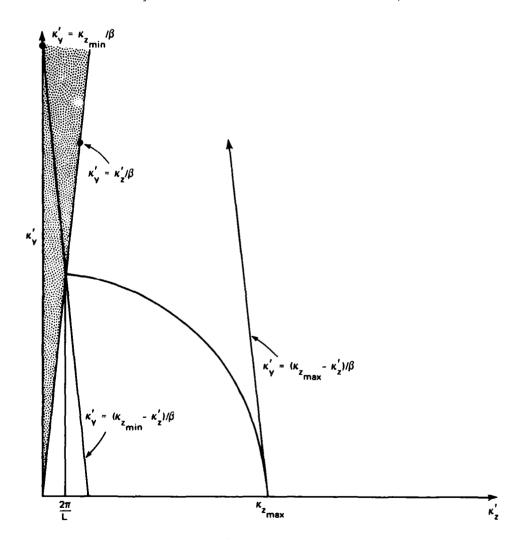


FIGURE 1 REGION OF κ_{γ}' - κ_{z}' PLANE WHERE 1/L|D_L| CAN BE APPROXIMATED BY sinc²

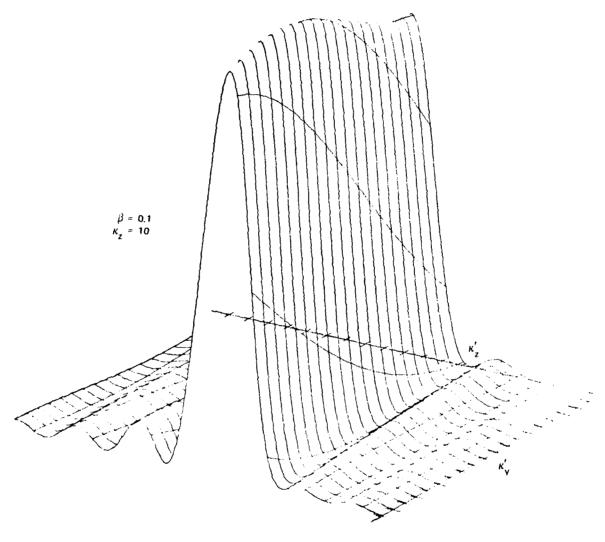


FIGURE 2 PERSPECTIVE PLOT SHOWING 1/L|D_L|^2 AS A FUNCTION OF κ_V^\prime AND κ_z^\prime FOR SMALL β AND LARGE κ_z

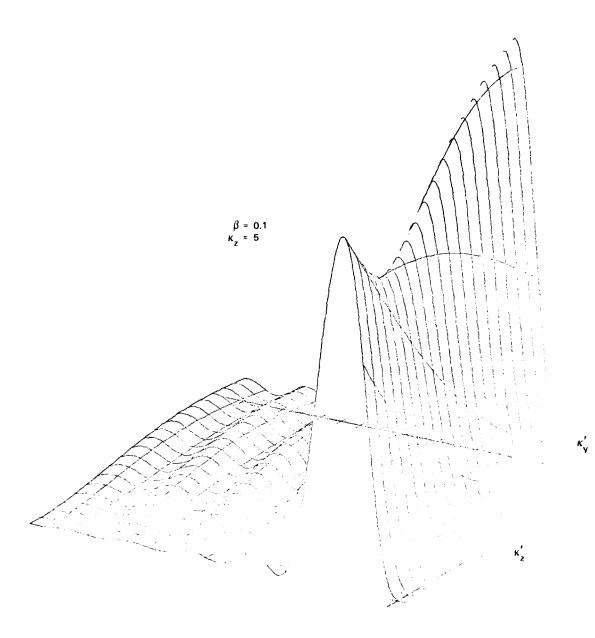


FIGURE 3 PERSPECTIVE PLOT SHOWING THE EFFECT OF DECREASING $\kappa_{\rm z}$

In Figure 3, the region where Eq. (26) breaks down is evident. The effect of increasing β is shown in Figure 4.

We have already established that the contribution to Eq. (14) for small κ_z' is negligible when $\kappa_z << 2\pi/L$. Thus, there is a minimum value of κ_z as shown in Figure 1. Beyond an arc drawn from the intersection of $\kappa_z' = 2\pi/L$ and $\kappa_y' = (\kappa_z - \kappa_z')/\beta$, the contribution to Eq. (14) of $\phi(\kappa', \kappa_z')/\kappa_z'^2$ must be negligible. We can then apply the sifting property of Eq. (26) to obtain

$$\hat{\Phi}_{\mathbf{z}}(\kappa_{\mathbf{z}}) \cong \int \int \frac{\Phi(\vec{\kappa}, \kappa_{\mathbf{z}} - \vec{\kappa}, \vec{\kappa})}{(\kappa_{\mathbf{z}} - \vec{\kappa}, \vec{\kappa})^{2}} \frac{d\vec{\kappa}}{(2\pi)^{2}} \cong \Phi_{1}(\kappa_{\mathbf{z}})/\kappa_{\mathbf{z}}^{2} . \tag{27}$$

The second approximation applied because $\kappa_z << \vec{\kappa}' \cdot \vec{\beta}$ in the region where Eq. (26) is valid. For a typical power-law SDF, the validity conditions for Eq. (27) are easily achieved $\beta < \cdot 4$.

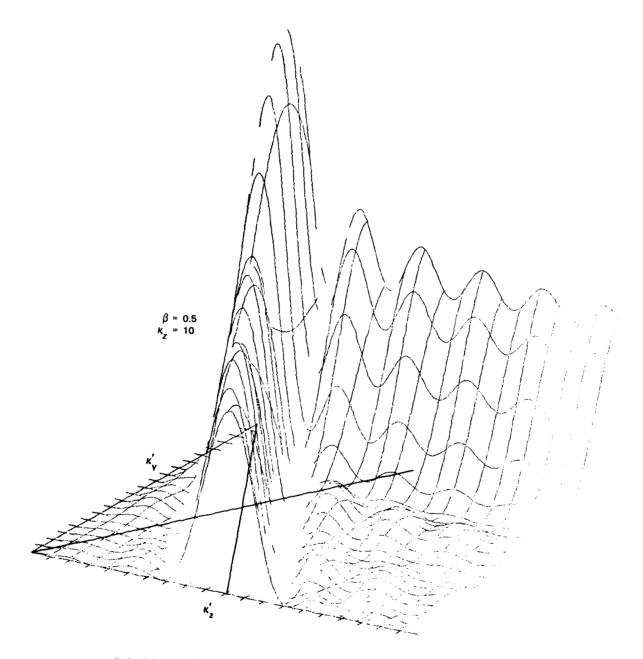


FIGURE 4 PERSPECTIVE PLOT SHOWING THE EFFECT OF INCREASING β

III DOPPLER SPECTRUM

A. Background

For some predictive scintillation codes, it is useful to model the Doppler spectrum of the complex signal, v(t). The Doppler spectrum is formally the Fourier transform of the mutual coherence function

$$R_{v}(\tau) = \langle v(t)v^{*}(t+\tau) \rangle \qquad . \tag{28}$$

Under reasonable assumptions, moreover, $\boldsymbol{R}_{\boldsymbol{V}}(\tau)$ admits the simple representation

$$R_{\mathbf{v}}(\tau) = \exp\left\{-\frac{1}{2}D_{\delta+}(\mathbf{v}_{eff}\tau)\right\} , \qquad (29)$$

where

$$D_{\delta,t}(y) = 2\sigma_{\delta,t}^{2} \left[1 - \rho_{\delta,t}(y) \right]$$
 (30)

is the phase structure function, σ_{δ_1} is the rms phase, and $\sigma_{\delta_1}(y)$ is the normalized phase autocorrelation function $[P_{\delta_2}(0)] = 1$. Equation (29) is strictly valid only in the plane normal to the propagation direction, that is, when parallel propagation effects are negligible. The correction factor that must be applied to accommodate parallel propagation effects are described in Rino, Section V, [1930]; thus, we shall only consider Eq. (29) here.

 $\label{thm:conditional} If the three-dimensional spatial SDF of the irregularities has \\$ the general power-law form

$$\frac{abC_{s}}{\left[q_{0}^{2} + q^{2}\right]^{1+1/2}},$$
(31)

then $\psi_{\mathcal{S}_1}(y)$, the two-dimensional Fourier transform of Eq. (31), can be evaluated as

$$q_{0y}(y) = \frac{2}{7(1-1/2)} \left| \frac{q_{0y}}{2} \right|^{\gamma-1/2} + \frac{1}{2} (q_{0y}),$$
 (32)

where y is a quadratic form in the spatial separation coordinates, $\frac{1}{x}$ and $\frac{1}{y}$, as described in Rino [1979a, b]. However, in spite of the comparatively simple form of Eq. (32), it is too cumbersome for direct use in Eq. (29), and we seek simpler approximate forms.

The simplest approximation that retains a dependence on the spectral index parameter, \cdot , is

$$D_{x_1}(y) \cong C_{x_1}^{-2} y^{(2)-1}$$
 , (33)

where $C_{\tilde{\beta},\sigma}^{-2}$ is the phase structure constant

$$C_{\delta_1}^2 = r_e^{2\sqrt{2}y} \frac{C_{\delta_1}}{2} \frac{2(1.5 - y)}{(0.5 + y)(2y - 1)2^{2y-1}}$$
, (34)

which is valid for $\gamma=1.5$. Equation (33) is obtained as an asymptotic approximation Eq. (30) in the limit as \mathbf{q}_0 becomes very small [Rino, 1979b]. Note that Eq. (33) does not retain an explicit dependence on \mathbf{q}_0 .

For more steeply sloped spectra ($\simeq 1.5$), a quadratic approximation of the form

$$D_{\hat{A}_{1}}(y) \cong D_{1}y^{2} \tag{35}$$

is admissible. In Eq. (35), D_1 is the first nonzero coefficient in a Taylor series expansion of $D_{\delta \varphi}(y)$. The expansion coefficients generally do not exist independently from an inner-scale cut-off, [Rino et al., 1980], although D_1 is independent of q_0 and q_i for $\nu > 1.5$.

For the entire range of ν values, $\boldsymbol{R}_{\boldsymbol{V}}(\tau)$ admits the approximate form

$$R_{v}(\tau) = \exp \left\{ -\frac{1}{2} C_{\delta \phi}^{2} |y|^{\min(2\nu-1,2)} \right\},$$
 (36)

where

$$\frac{2\pi c_{\delta\phi}^{2}}{c_{p}^{2}} = \begin{cases}
\frac{2(1.5 - v)}{\Gamma(0.5 + v)(2v - 1)v^{2v-1}} & 0.5 < v < 1.5 \\
-\frac{1}{2}\log(q_{1}/q_{0}) & v = 1.5 \\
\frac{\Gamma(v - 1.5)}{4\Gamma(v - 0.5)} & v > 1.5
\end{cases}$$
(37)

A plot of $2\pi C_{\delta \varphi}^{2}/C_{p}$ as a function of ν is illustrated in Figure 5. The singular behavior at $\nu=1.5$ is indicative of a breakdown in both the asymptotic and quadratic approximations. The dashed line is probably closer to the correct functional dependence of an asymptotic approximation of the form of Eq. (32).

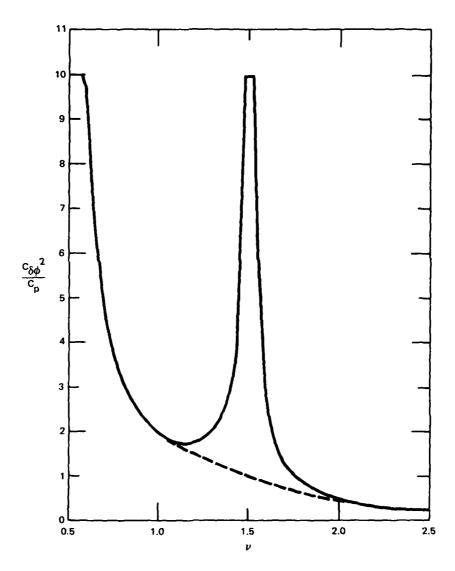


FIGURE 5 VARIATION OF STRUCTURE FUNCTION EXPANSION COEFFICIENT WITH CHANGING SPECTRAL INDEX

For predictive modeling, therefore, it is convenient to take

$$2 \cdot c_{\text{pl}}^{2} / c_{\text{p}} \cong 2^{2} - 4.5 \times + 5.5 + 1.0 \le 2 \le 2.0$$
 (38)

which follows the dashed curve in Figure 5 very closely. Approximations such as Eq. (38), are particularly convenient because of the evidence that the spectral index itself varies systematically with changing turbulent strength [Livingston et al., 1980; Rino et al., 1980c]. In any case, for our purposes here, we are only interested in the behavior of Eq. (36) as a function of .. Because of the simple power-law form of the argument of the exponential function, C is effectively only a scale factor.

B. Special Cases and Numerical Computations

To compute the Doppler spectrum, we must evaluate the integral

$$\Phi(f) = \int R_{\mathbf{v}}(\tau) \exp \left\{-2\pi i f \tau\right\} d\tau \qquad (39)$$

Substituting $y = v_{eff}^{\tau}$ into Eq. (36) gives

$$R_{v}(\tau) = \exp \left\{-\left|\frac{\pi}{\tau_{0}}\right|^{\min(2\tau-1,2)}\right\}$$
 (40)

where

$$r_0 = \frac{1}{v_{eff}} \left(\frac{2}{c_{of}^2}\right) \frac{1}{\min(2^{-1}, 2)}$$
 (41)

If = 1, Eq. (39) admits the exact solution

$$(f) = \frac{1}{10} \frac{2}{1 + (2\pi t_0 f)^2} . \tag{42}$$

Similarly, if = 1.5, then $\frac{1}{2}(f)$ takes the Gaussian form

$$(f) = \sqrt{\frac{1}{10}} \exp \left\{ -\frac{(2^{-1}0^{-1})^{2}}{4} \right\} \qquad (43)$$

Thus, the general trend is from shallow power-law to Gaussian as γ increases.

This is verified in the numerical evaluations of Eq. (39) using the fast Fourier transform algorithm. In Figure 6, $\tau_0 \psi(f)$ is plotted for $\gamma=0.8$, $\gamma=0.9$, and $\gamma=1.0$. For such shallowly sloped phase spectra, the overall shape of $\psi(f)$ changes little. As the slope increases, however, shape changes rapidly—as shown in Figure 7 where $\tau_0 \psi(f)$ is plotted for $\gamma=1.3$, $\gamma=1.4$, and $\gamma=1.5$.

For predictive modeling, therefore, we can use Eq. (42), where the spectral index is comparatively small, and Eq. (43) for the opposite extreme. It should be kept in mind, however, that τ_0 itself depends on the spectral index parameter, τ , as well as on the perturbation strength.

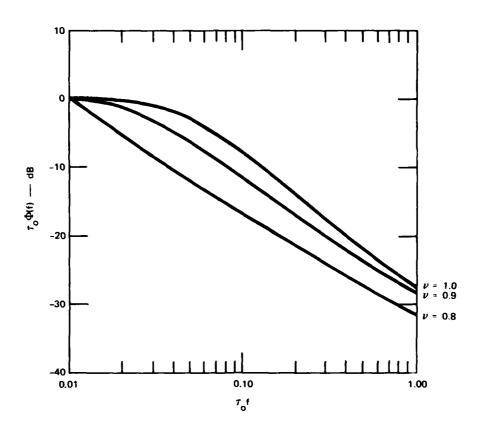


FIGURE 6 DOPPLER SPECTRUM FOR SHALLOWLY SLOPED PHASE SPECTRA

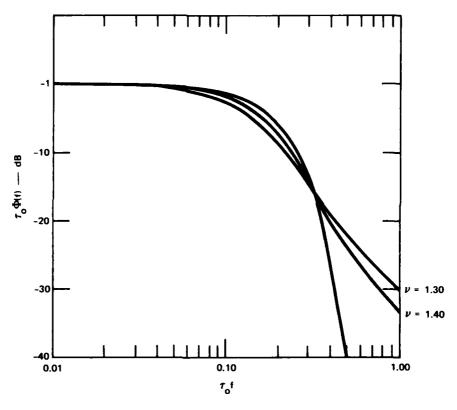


FIGURE 7 DOPPLER SPECTRUM FOR MORE STEEPLY SLOPED PHASE SPECTRA

IV CONCLUSIONS

In this report we developed a theory to interpret beacon-phase data when the line-of-sight velocity component is much larger than the transverse component. In that situation, there is a simple relationship between the phase spectral-density function and the one-dimensional in-situ spectral-density function that a rocket-borne density probe would be measured. Thus, both the spectral shape and the turbulent strength can be determined.

Because the rocket beacon signal itself is the data source, no telemetry is required. Thus, such beacon measurements provide a comparatively inexpensive means for obtaining quantative ionospheric structure measurements.

Also, a simple mathematical model was developed for predicting the Doppler spectrum of a satellite signal received in the usual situation in which the transverse Doppler component dominates. This model is useful both for data interpretation and system analysis.

Most other theoretical results of interest have been verified. The mutual coherence function model itself, which is the starting point for the Doppler spectrum computations, has not yet been tested against real data, but this effort is being pursued under a separate contract.

REFERENCES

- Berning, W. W., "Charge Densities in the Ionosphere from Radio Doppler Data," J. of Meteor., Vol. 8, p. 176 (1951).
- Crane, R., "Ionospheric Scintillation," Proc. IEEE, Vol. 65, No. 2, p. 180 (1977).
- Davies, K., R. B. Fritz, R. N. Grubb, and J. E. Jones, "Some Early Results from the ATS-6 Radio Beacon Experiments," Radio Science, Vol. 10, p. 785 (1975).
- Flatte, S. M., R. Dashen, W. H. Munk, and F. Zachariasen, "Sound Transmission Through a Fluctuating Ocean," (Cambridge, 1979).
- Livingston, R. C., C. L. Rino, J. P. McClure, and W. B. Hanson, "Spectral Characteristics of Medium-Scale Equatorial F-Region Irregularities," J. Geophys. Res., Accepted for Publication (1980).
- Petriceks, J., "Rocket RF-Beacon Experiment for the Summer 1979 Kwajalein Campaign," <u>Proceedings of the Summer Equatorial</u> Experiment Data Review Meeting (March 1980).
- Rino, C. L., "A Power-Law Phase Screen Model for Ionospheric Scintillation 1. Weak Scatter," <u>Radio Science</u>, Vol. 14, No. 6, p. 1135 (1979).
- Rino, C. L., "A Power-Law Phase Screen Model for Ionospheric Scintillation 2. Strong Scatter," <u>Radio Science</u>, Vol. 14, No. 6, p. 1147 (1979b).
- Rino, C. L., "Propagation Modeling and Evaluation of Communication System Performance in Nuclear Environments," DNA 5265F, Final Report, Contract DNA001-77-C-0038, SRI Project 5960, SRI International, Menlo Park, CA. (February 1980).
- Rino, C. L., V. H. Gonzales, A. R. Hessing, "Coherence Bandwidth Loss in Transionospheric Radio Propagation," Topical Report, Contract DNA001-80-C-0077, SRI Project 1284, SRI International, Menlo Park, CA. (March 1980a).
- Rino, C. L., R. C. Livingston, B. C. Fair, M. D. Cousins, "Continued Performance of the Wideband Satellite Experiment," Final Report, Contract DNA001-77-C-0220, SRI Project 6434, SRI International, Menlo Park, CA. (June 1980b).

Rino, C. L., R. T. Tsunoda, J. Petriceks, R. C. Livingston, M. C. Kelley, and K. D. Baker, "Simultaneous Rocket-Borne Beacon and In-Situ Measurements of Equatorial Spread F-Long Wavelength Results," J. Geophys. Res., Accepted for Publication (1980).

Rosenblatt, M., Random Processes (Oxford Press, N.Y., 1962).

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